

Boosting:

**A weighted crowd of
narrowminded
experts**

Aaron & Dylan

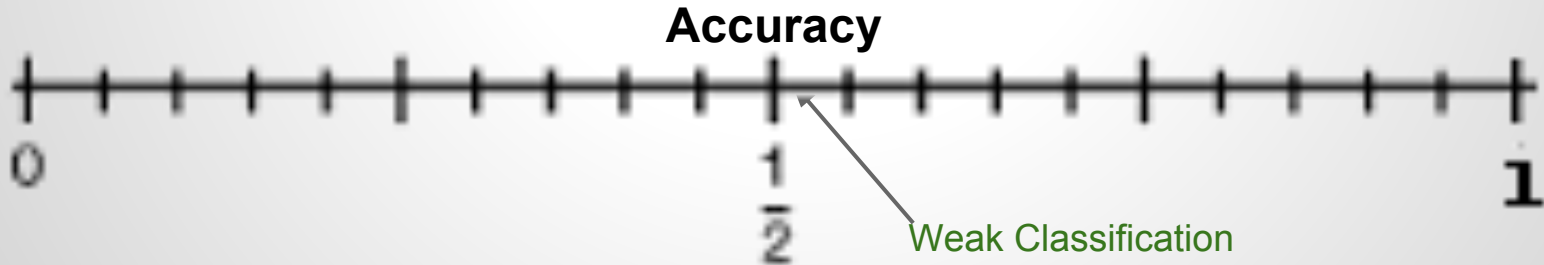


Boosting Hypothesis (Kearns, Valiant; 1988-89)

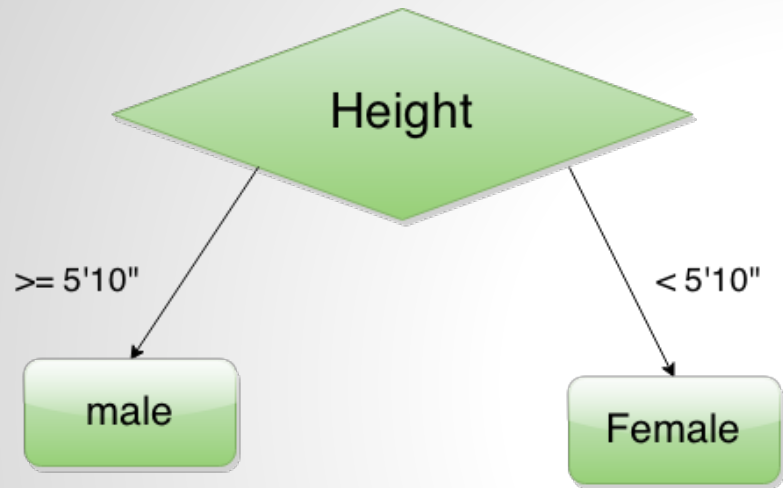
We can make a strong classifier (arbitrarily well at classification) from a collection of weak classifiers (somewhat better than random guess).

Weak Classifiers

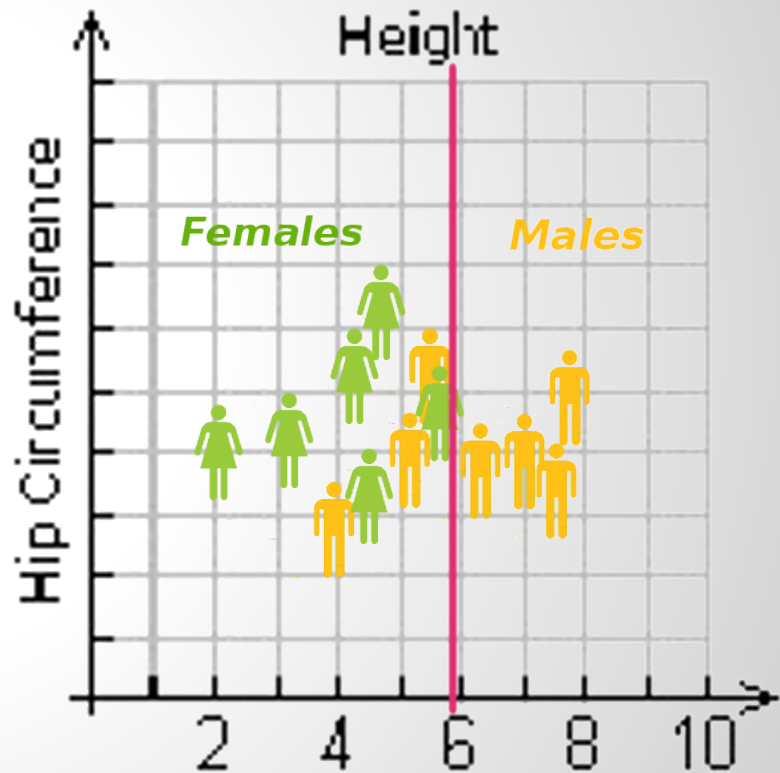
- Classifier which may be only slightly correlated with true classification (accuracy > 50%)
- Examples: Naïve Bayes, logistic regression, decision stumps



Decision Stumps

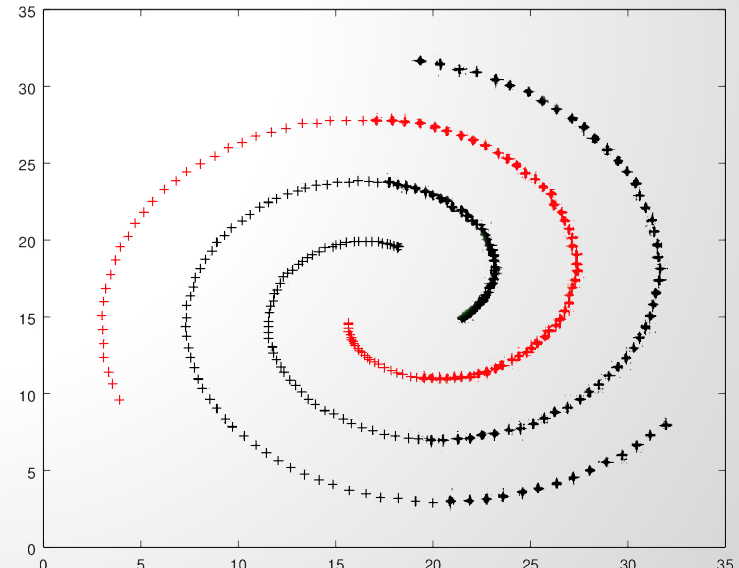
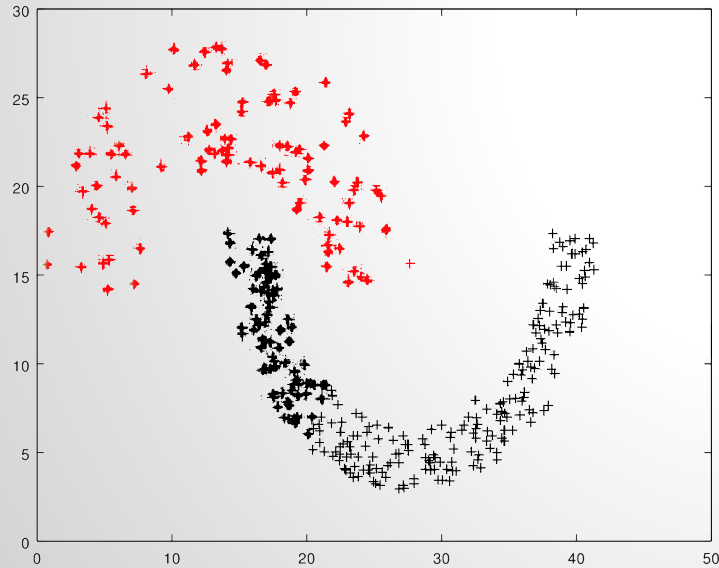


- Single Level Decision Tree
- Focus on a single feature dimension
- Create a decision boundary along that dimension

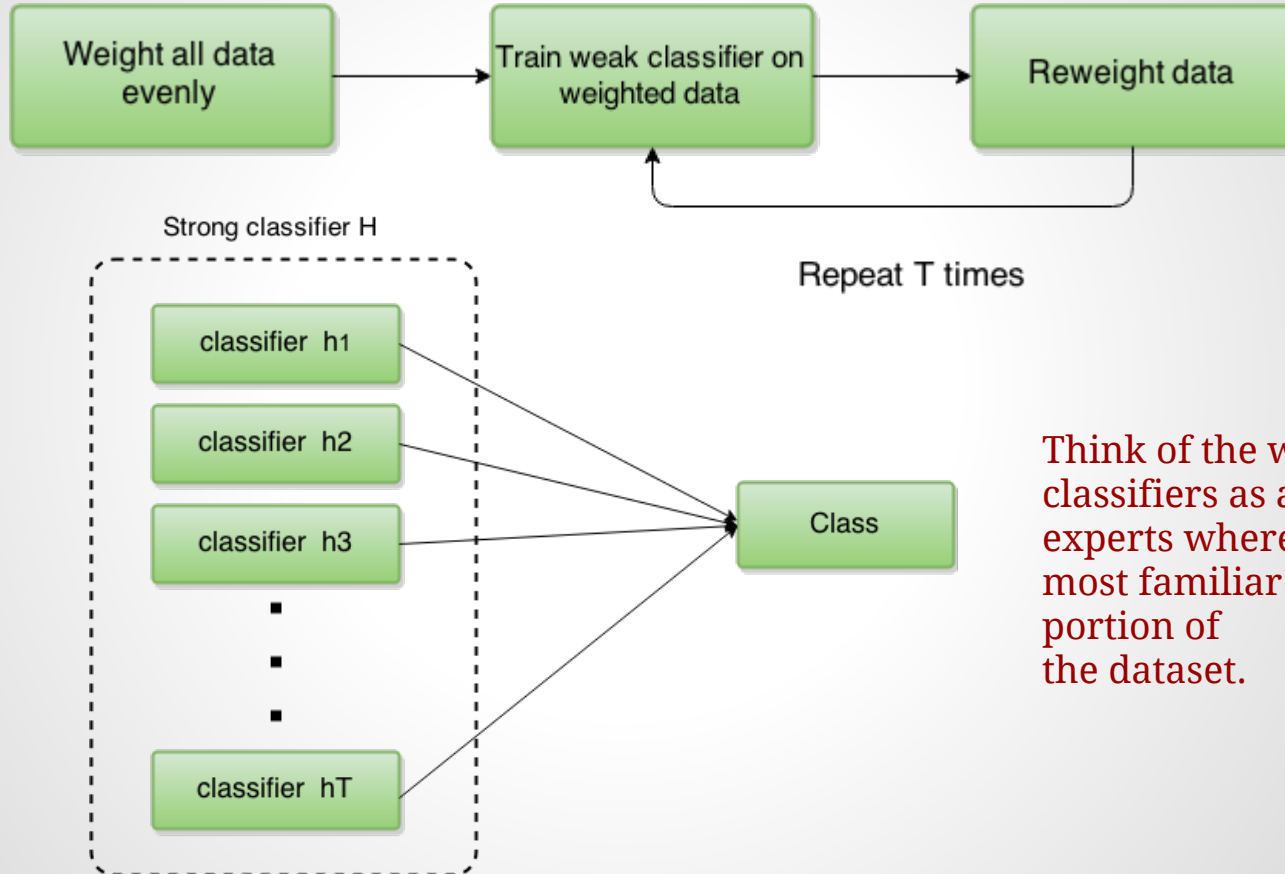


Advantages of Boosting:

- Easy and fast to train weak classifiers
- Simple models don't usually overfit
- Weak classifiers can not solve hard problems



Boosting: The Basic Idea



Think of the weak classifiers as a crowd of experts where each is most familiar with some portion of the dataset.

AdaBoost: Boosting for Binary Classification

Suppose dataset: $(x_1, y_1), \dots, (x_N, y_N)$

where $x_i \in \mathbb{R}^n, y_i \in Y = \{-1, 1\}$

Let $D_t(i) =$ weight of point x_i

Goal: Build classifier $H(x) = \text{sign}(\alpha_1 h_1(x) + \dots + \alpha_T h_T(x))$

where $h_1(x), \dots, h_T(x)$ are binary classifiers,
built on distributions D_1, \dots, D_T respectively.

Issue: How to find the best α 's and D 's.

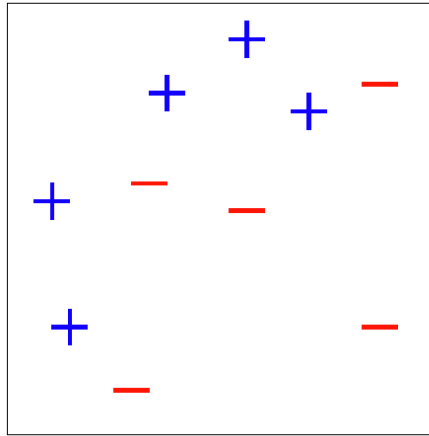
Answer: Iteratively minimize exponential loss:

If $F(x) = \alpha_1 h_1(x) + \dots + \alpha_T h_T(x)$, then

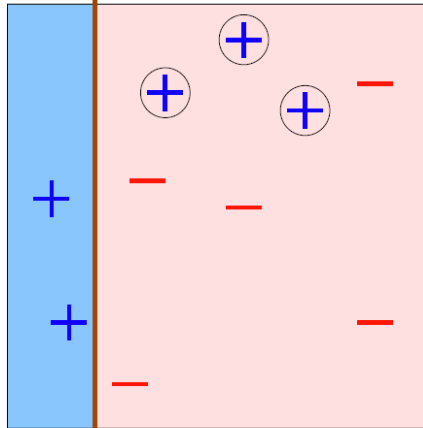
$$L = \frac{1}{N} \sum_{i=1}^T \exp(-y_i F(x_i))$$

AdaBoost with Decision Stumps as Weak Classifiers

(Shapire, Freund. 1999)



D_1



$h_1(x)$

Round One:

Build h_1 on distribution D_1

Then calculate:

$$\epsilon_1 = \Pr_{i \sim D_1}(h_1(x) \neq y_i).$$

(sum of misclassified point weights)

Next calculate α_1 .

Then calculate D_2 .

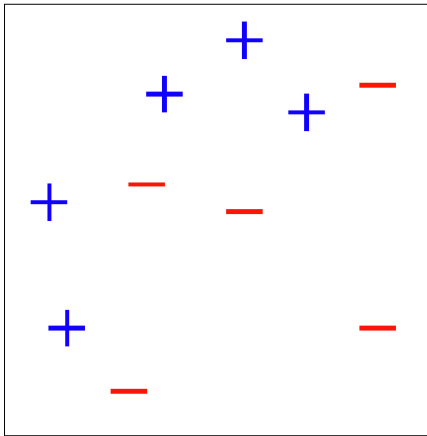
$t = 1, \dots, T$

Train weak classifier
 $h_t : \mathbb{R}^n \rightarrow R$
on distribution D_t

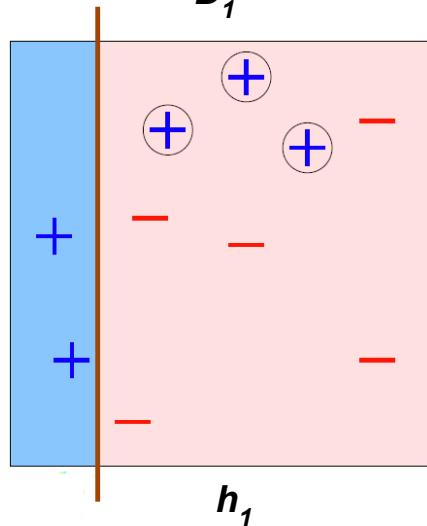
Pick α_t
(weight for h_t)
$$\alpha_t := \frac{1}{2} \ln\left(\frac{1 - \epsilon_t}{\epsilon_t}\right)$$

Set $D_{t+1}(i) :=$
$$\frac{D_t(i) \exp(-\alpha_t y_i h_t(x_i))}{Z_t}$$

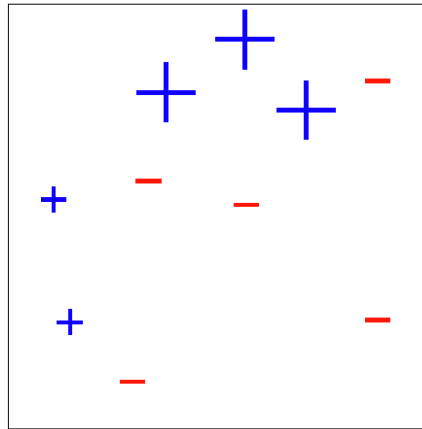
$$H(x) := \text{sign}\left(\sum_{t=1}^T \alpha_t h_t(x)\right)$$



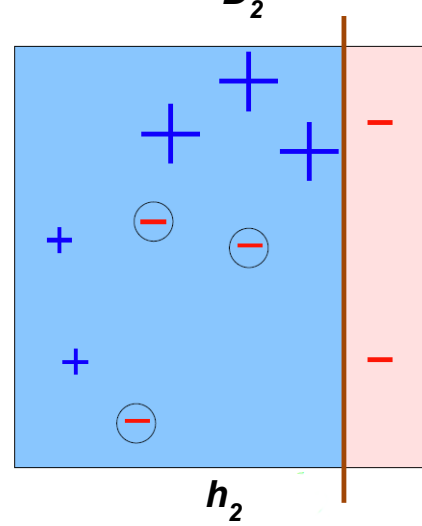
D_1



h_1



D_2



h_2

Round One:

Build h_1 on distribution D_1

$$\varepsilon_1 = 3/10$$

$$\alpha_1 = 0.42$$

$D_2(i) = 0.166$ for x_i that were misclassified

$D_2(i) = 0.072$ for x_i that were correctly classified

Round Two:

Build h_2 on distribution D_2

$$\varepsilon_2 = 0.216$$

$$\alpha_2 = 0.65$$

$$\varepsilon_2 = 0.216, \quad \alpha_2 = 0.65$$

For each X_i where:

h_1 was wrong, h_2 was right:

$$D_3(i) = 0.11, \quad D_2(i) = 0.166$$

h_1 was right, h_2 was wrong:

$$D_3(i) = 0.175, \quad D_2(i) = 0.072$$

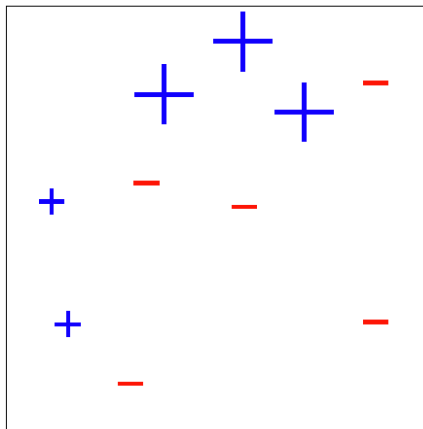
h_1 was right, h_2 was right:

$$D_3(i) = 0.047 \quad D_2(i) = 0.072$$

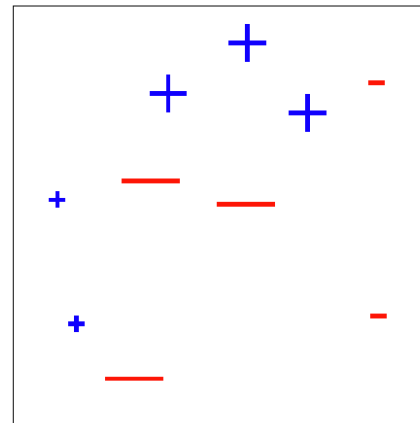
Round Three:

Train h_3 on D_3

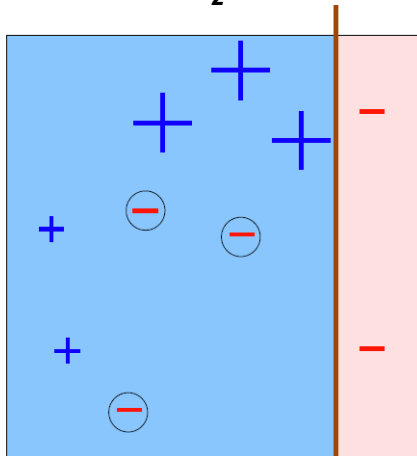
$$\varepsilon_3 = 0.144, \quad \alpha_3 = 0.91$$



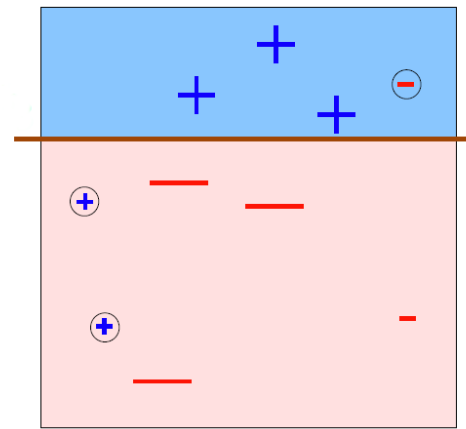
D_2



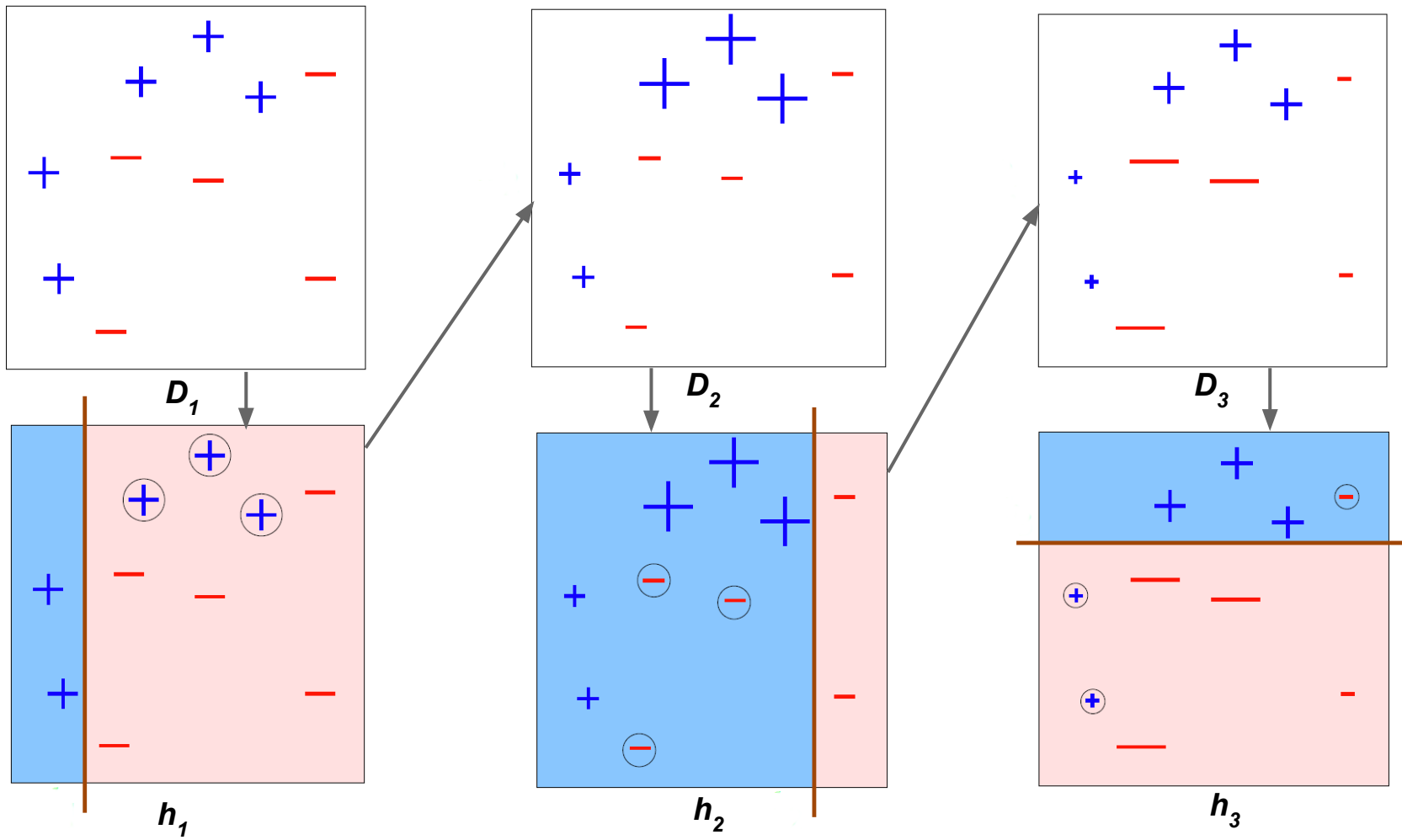
D_3



h_2



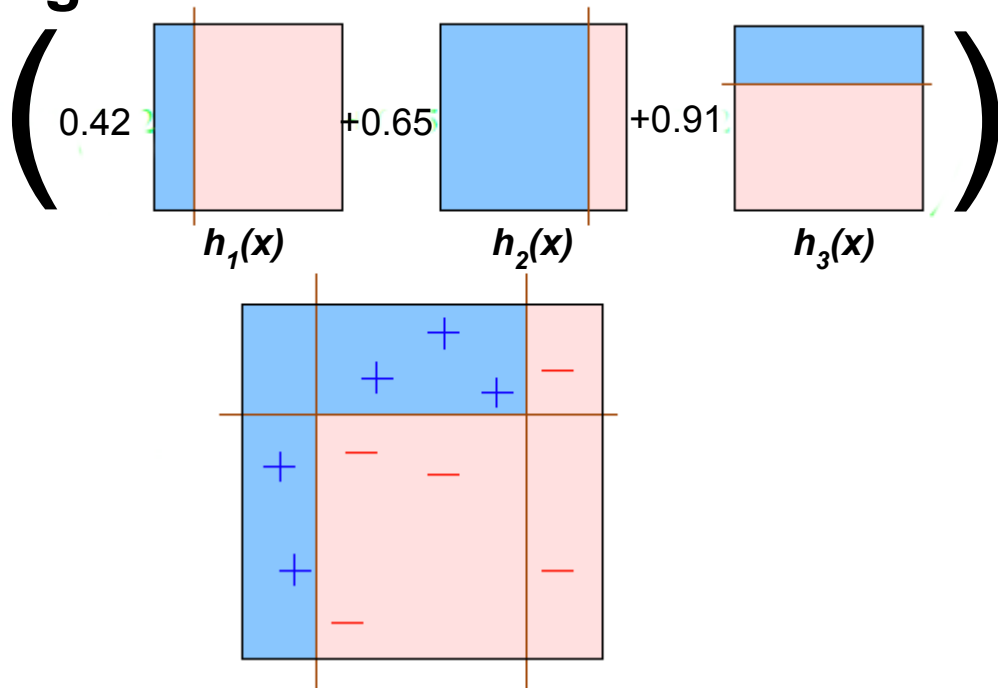
h_3



Strong Classifier

$H(x)$

sign



$t = 1, \dots, T$

Train weak classifier
 $h_t : \mathbb{R}^n \rightarrow R$
on distribution D_t

Pick α_t
(weight for h_t)

$$\alpha_t := \frac{1}{2} \ln\left(\frac{1 - \epsilon_t}{\epsilon_t}\right)$$

Set $D_{t+1} :=$

$$\frac{D_t(i) \exp(-\alpha_t y_i h_t(x_i))}{Z_t}$$

$$H(x) := \text{sign}\left(\sum_{t=1}^T \alpha_t h_t(x)\right)$$

Boosting Demos

Swirly boosting demo

More Swirly boosting demo

AdaBoost in action

References:

Schapire, R. E. (2003). The boosting approach to machine learning: An overview. In *Nonlinear estimation and classification* (pp. 149-171). Springer New York.

Schapire, R. E. (1990). The strength of weak learnability. *Machine learning*, 5(2), 197-227.

Kearns, M. (1988). Thoughts on hypothesis boosting. *Unpublished manuscript*, 45, 105.

Long, P. M., & Servedio, R. A. (2010). Random classification noise defeats all convex potential boosters. *Machine Learning*, 78(3), 287-304.

Freund, Y., & Schapire, R. E. (1995, January). A decision-theoretic generalization of on-line learning and an application to boosting. In *Computational learning theory* (pp. 23-37). Springer Berlin Heidelberg.

[MIT Boosting Lecture](#)

Software:

[Wikipedia list from AdaBoost page](#)

[Boosting Song](#)